TOULON

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Exploring Deep Learning through Flux.jl: Insights into Core Mechanisms and Datasets

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1 Introduction

- 2 Core Mechanisms
- 3 Flux Built-in Layers
- 4 Datasets For Deep Learning
- 5 Showcase of CNN and Transformers



3 Flux Built-in Layers

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What is Deep Learning?

• A subset of machine learning where artificial neural networks, algorithms inspired by the human brain, learn from large amounts of data.



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- Ability to learn and improve from experience without being explicitly programmed.

What is Deep Learning?

- A subset of machine learning where artificial neural networks, algorithms inspired by the human brain, learn from large amounts of data.
- Ability to learn and improve from experience without being explicitly programmed.
- Efficient in processing large datasets and recognizing patterns.



3 Flux Built-in Layers

4 Datasets For Deep Learning

5 Showcase of CNN and Transformers

Flux.jl is a comprehensive package within the Julia programming ecosystem, designed specifically for deep learning applications.

• Open source Julia package dedicated to deep learning.



Michael Innes et al. Fashionable Modelling with Flux CoRR, 2018 FluxAl Flux, The Elegant Machine Learning Stack https://fluxml.ai/

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- Full support for GPU utilization and Automatic Differentiation.

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Flux.jl is a comprehensive package within the Julia programming ecosystem, designed specifically for deep learning applications.

- Open source Julia package dedicated to deep learning.
- Full support for GPU utilization and Automatic Differentiation.
- Wide array of tools for efficient data processing.
- Vast selection of predefined layers for various neural network architectures.



- Decomposition of complex nested structures
- Automatic reverse differentiation
- Descent-based minimization methods

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The core mechanisms of Flux are the following:

• Decomposition of complex nested structures (Functors.jl)

FluxML Functors.jl https://github.com/FluxML/Functors.jl

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- Decomposition of complex nested structures (Functors.jl)
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The core mechanisms of Flux are the following:

- Decomposition of complex nested structures (Functors.jl)
- Automatic reverse differentiation (Zygote.jl)
- Descent-based minimization methods (Optimisers.jl)

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Decomposition of complex nested structures

- Automatic reverse differentiation
- Descent-based minimization methods
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 Nested structures are commonly employed in deep learning, primarily due to their efficiency in data processing.



Decomposition of complex nested structures

• Goal : Facilitate access to the parameters that need optimization.

```
using Flux, Flux. Functors J
struct Linear{T1<:Real,T2<:Function}</pre>
    W :: Matrix {T1}
    b ::Vector{T1}
    f :: T2
end 🖌
@functor Linear 🗸
struct Chain
    lavers ::Vector{Linear}
end 🗸
@functor Chain /
Linear(n,m,f) = Linear(randn(m,n),randn(m),f); 
model = Chain([
   Linear(1,64,tanh),
    Linear(64,64,tanh),
    Linear(64,64,tanh),
    Linear(64,1,identity)
 lux.params(model) .|> length |> sum |8513
```

Decomposition of complex nested structures

- Goal : Facilitate access to the parameters that need optimization.
- Limitation : All parameters must be stored on the heap.

```
using Flux,Flux.Functors 🗸
struct Linear{T1<:Real,T2<:Function}</pre>
    W :: Matrix {T1}
    b ::Vector{T1}
    f :: T2
end 🖌
@functor Linear 🗸
struct Chain
    layers ::Vector{Linear}
end 🗸
@functor Chain 
Linear(n,m,f) = Linear(randn(m,n),randn(m),f); //
model = Chain([
    Linear(1,64,tanh),
    Linear(64,64,tanh),
    Linear(64,64,tanh),
    Linear(64,1,identity)
  lux.params(model) .|> length |> sum |8513
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Automatic differentiation

• Computational technique used to calculate the gradient of a function relative to its inputs.

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Automatic differentiation

- Computational technique used to calculate the gradient of a function relative to its inputs.
- ForwardDiff : Forward mode (Number of inputs < Number of outputs).
- Zygote : Forward mode (Number of inputs > Number of outputs).

using Flux.Zygote \[\]
f(x) = 2. * x.^2 \|> sum; \[\]
x = rand(3); \[\]
gradient(f,x)[1] == 4 .* x \[true

Mixing Zygote and Functors

• Zygote is capable of differentiating nested structures, provided they are appropriately tagged by Functors. (l::Linear)(x) = l.f.(muladd(l.W,x,l.b)) \/
model = Linear(100,1,identity); \/
compute_model(model,x) = model(x)[1]; \/
x = rand(100); \/
g = gradient(compute_model,model,x); \/
g[1].W \lx100 Matrix{Float64}:
g[1].b \l-element Vector{Float64}:



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• Basic Descent Method:

```
• f: \mathbb{R}^n \to \mathbb{R} at least C^1,
```

```
using Flux.Zygote 🗸
using Flux.Optimisers 🗸
struct DescentAlg <: Optimisers.AbstractRule</pre>
    d :: Float64
end 🗸
function Optimisers.apply!(o::DescentAlg, state, x, \bar{x})
    new⊼ = o.α.∗⊼
    nextstate = state + 1
    return nextstate, newx
end 🖌
Optimisers.init(o::DescentAlg, x::T) where T = 1 | J
opt_rule = DescentAlg(0.1); /
x = rand(3); \downarrow
opt = Optimisers.setup(opt_rule, x); /
f(x) = 2. * x.^2 > sum; J
f(x) 0.3587933958011746
for _ in 1:10
    Optimisers.update!(opt,x,gradient(f,x)[1]);
end 🤳
f(x) 1.3118055022973196e-5
```

• Basic Descent Method:

- $f: \mathbb{R}^n \to \mathbb{R}$ at least C^1 ,
- $x \in \mathbb{R}^n$,

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opt = Optimisers.setup(opt_rule, x); /
f(x) = 2. * x.^2 > sum; J
f(x) 0.3587933958011746
for _ in 1:10
   Optimisers.update!(opt,x,gradient(f,x)[1]);
end J
f(x) 1.3118055022973196e-5
```

• Basic Descent Method:

- $f: \mathbb{R}^n \to \mathbb{R}$ at least C^1 ,
- $x \in \mathbb{R}^n$,
- x^k such that,

 $x^{k+1} = x^k - \alpha \nabla f(x^k),$

where α is the step size.

```
using Flux.Zygote 🗸
using Flux.Optimisers 🗸
struct DescentAlg <: Optimisers.AbstractRule</pre>
    a :: Float64
end J
function Optimisers.apply!(o::DescentAlg, state, x, x)
    nextstate = state + 1
    return nextstate, newx
end J
Optimisers.init(o::DescentAlg, x::T) where T = 1 1
opt_rule = DescentAlg(0.1); /
x = rand(3); \sqrt{}
opt = Optimisers.setup(opt_rule, x); /
f(x) = 2. * x.^2 > sum; J
f(x) 0.3587933958011746
for in 1:10
    Optimisers.update!(opt,x,gradient(f,x)[1]);
end 🌙
    1.3118055022973196e-5
```

- Basic Descent Method:
- Adam Method :

 $egin{array}{rcl} m^{k+1}&=&eta_1m^k\ &+(1-eta_1)
abla f(x^k) \end{array}$

$$v^{k+1} = eta_2 v^k + (1-eta_2)
abla f(x^k)^2$$

$$x^{k+1} = x^k - \frac{\alpha m^{k+1}}{(1-(\beta_1)^k)(\sqrt{rac{\nu^{k+1}}{1-(\beta_2)^k}}+\varepsilon)}$$

where α is the step size, β_1 , β_2 and ε are parameters.

Mixing Optimisers, Zygote and Functors

 Optimisers is capable of optimizing nested structures, provided they are appropriately tagged by Functors.

```
(l::Linear)(x) = l.f.(muladd(l.W.x.l.b)) /
model = Linear(100,1,identity); 
compute_model(model.x) = model(x)[1]; 
x = rand(100); J
opt_rule = AdamAlg(a= 0.1); /
opt = Optimisers.setup(opt_rule, model); //
model(x)[] -4.991810896328357
for in 1:10
   g = gradient(compute_model,model,x)[1];
   Optimisers.update!(opt,model,g);
end 🗸
model(x)[1] -58.87701713966101
```



3 Flux Built-in Layers

- Basic Flux Examples with Dense Layers
- The Convolution Layer
- The MultiHeadAttention(MHA) Layer

4 Datasets For Deep Learning

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• The Dense Layer or fully connected layer : Connects every neuron in one layer to every neuron in the next layer.

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- The Convolution Layer for image processing : Applie a convolution operation to the input, passing the result to the next layer.

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- The Dense Layer or fully connected layer : Connects every neuron in one layer to every neuron in the next layer.
- The Convolution Layer for image processing : Applie a convolution operation to the input, passing the result to the next layer.
- The Normalizing Layer or the batch normalization : Improve model stability and reduce overfitting by normalizing layer inputs.
- The Multi-Head Attention Layer for processing sequential data (ex : text) : Multiple dense layers devided in key, query and value.



3 Flux Built-in Layers Basic Flux Examples with Dense Layers The Convolution Layer The MultiHeadAttention(MHA) Layer

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• The linear regression model is a Dense Layer with only one neuron. In this setup, the identity function is used as the activation function.

using Flux 🗸
model = Flux.Dense <mark>(</mark> 1,1,identity <mark>)</mark> ; 🗸
f(x) = x^3-x^2+x+2; /
N=1000; J
x = rand(-1:0.01:1,1,N); \
y = f.(x); J
<pre>loss(model,x,y) = Flux.mse(model(x),y); </pre>
loss(model,x,y) 2.9885269487981727

- The linear regression model is a Dense Layer with only one neuron. In this setup, the identity function is used as the activation function.
- The primary objective in this model is to minimize the mean squared error (MSE), which is the loss function.

using Flux 🗸
<pre>model = Flux.Dense(1,1,identity); </pre>
f(x) = x^3-x^2+x+2; /
N=1000; J
x = rand(-1:0.01:1,1,N); V
y = f.(x); /
<pre>loss(model,x,y) = Flux.mse(model(x),y); </pre>
loss(model,x,y) 2.9885269487981727

 The built-in layers, such as Dense, are Functors by default in many deep learning frameworks.

```
N=1000; J
epoch = 100; /
x = rand(-1:0.01:1,1,N); /
v = f(x): J
loss(model,x,y) = Flux.mse(model(x),y); /
loss(model,x,y) 4.0829329362030355
opt_rule = Flux.Adam(0.1); 
opt = Flux.setup(opt_rule, model); //
for _ in 1:epoch
    g = gradient(loss,model,x,y)[1];
    Flux.update!(opt,model,g);
end 🗸
loss(model,x,y) 0.12288050564779106
```

- The built-in layers, such as Dense, are Functors by default in many deep learning frameworks.
- In this context, *N* represents the number of training examples, and 'epoch' refers to the number of iteration for the optimization process.

```
N=1000; /
epoch = 100; /
x = rand(-1:0.01:1,1,N); /
v = f(x): J
loss(model,x,y) = Flux.mse(model(x),y); /
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Exemple of convolution operation on matricies

- Let *M* be a 3x3 matrix, and *F* a 2x2 filter.
- We apply F to M to compute the resulting matrix N.
- The convolution involves element-wise multiplications and summations.
- Here, we demonstrate the computation of the first element of *N*.

$$M = \begin{bmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{bmatrix} \quad F = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix} \quad N = \begin{bmatrix} N_{11} & N_{12} \\ N_{21} & N_{22} \end{bmatrix}$$

 $N_{11} = M_{11} \cdot F_{11} + M_{12} \cdot F_{12} + M_{21} \cdot F_{21} + M_{22} \cdot F_{22}$

Define the convolution layer at hand

• Suppose we have a $n \times m$ matrix M and a $l \times k$ filter Fwith a padding of (p_1, p_2) and a stride of (s_1, s_2) .

```
struct MyConv
F ::Array
D ::Donse
pad ::Tuple
stride ::Tuple
end v
@functor MyConv v
function MyConv(1 ::Tuple,n,m,f ::T1;pad=(0,0),
stride=(1,1)) where T1<;Function
D = Flux.Dense(n=>m,f)
MyConv(randn(T...,n),D,pad,stride)
end; v
model = MyConv((3,3),1,3,tanh,pad=(1,1)); v
```

Define the convolution layer at hand

- Suppose we have a $n \times m$ matrix M and a $l \times k$ filter Fwith a padding of (p_1, p_2) and a stride of (s_1, s_2) .
- Then the operation is,

 $N_{ij} = M_{(i-1)s_1+m,(j-1)s_2+n}F_{m,n}$

```
ction padarray(A::Array, pad::Tuple)
   original dims = size(A)
   new_dims = original_dims[1:2] .+ 2 .* pad
   B = zeros(eltype(A), new_dims...,original_dims[3:end]...)
   indices = [p+1:p+d for (p, d) in zip(pad, original_dims[1:2])]
   B indices....: = A
   roturn R
   padarray (generic function with 1 method)
function (model ::MyConv)(x)
   P1, P2 = model.pad
   S1.S2 = model.stride
   xpad = padarray(x, (P1, P2))
   F = model.F
   @tullio C[i, j,k,l] := xpad[(i-1)*$S1 + m, (j-1)*$S2 + n,k,l]
   * F[m, n,k]
   return permutedims(model.D(permutedims(C, [3,1,2,4])), [2,3,1,4])
```

Define the convolution layer at hand

- Suppose we have a $n \times m$ matrix M and a $l \times k$ filter Fwith a padding of (p_1, p_2) and a stride of (s_1, s_2) .
- N will be of dimention $\frac{n+2p_1-l}{s_1} + 1 \text{ by } \frac{m+2p_2-k}{s_2} + 1.$

```
nction padarray(A::Array, pad::Tuple)
    original dims = size(A)
    new_dims = original_dims[1:2] .+ 2 .* pad
   B = zeros(eltype(A), new_dims...,original_dims[3:end]...)
   indices = [p+1:p+d for (p, d) in zip(pad, original_dims[1:2])]
    B indices....: = A
    roturn B
end padarray (generic function with 1 method)
function (model ::MyConv)(x)
   P1,P2 = model.pad
   S1.S2 = model.stride
    xpad = padarray(x, (P1, P2))
    F = model.F
   @tullio C[i, j,k,l] := xpad[(i-1)*$S1 + m, (j-1)*$S2 + n,k,l]
    * F[m, n,k]
    return permutedims(model.D(permutedims(C,[3,1,2,4])),[2,3,1,4])
```

• Far More Optimized (2 times less allocations)

```
using Flux  
model = Conv((3,3),1=>3,tanh,pad=(1,1));  
xtest = rand(32,32,1,100);  
model(xtest) 32×32×3×100 Array{Float32, 4}:
```



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• Three principal components: Value, Key, Query.



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- Split into *h* parts and pass them through dense layers.



- Three principal components: Value, Key, Query.
- Split into *h* parts and pass them through dense layers.
- Attention for each head :

 $\mathsf{Attention} = \mathsf{softmax}$

$$\left(\frac{QK'}{\sqrt{dim_k}}\right)V,$$



- Three principal components: Value, Key, Query.
- Split into *h* parts and pass them through dense layers.
- Attention for each head :

А

ttention = softmax
$$\left(\frac{QK^T}{\sqrt{dim_{\mu}}}\right)$$



```
struct MHA
    0 ::Dense
    K ::Dense
    V ::Dense
    D ::Dense
    nheads :: Int
end 🗸
function MHA(g_dim,k_dim,v_dim,gkv_dim,
out_dim.nheads)
    @assert g_dim % nheads == 0
    @assert v dim % nheads == 0
    @assert k_dim == g_dim
    @assert gkv_dim % nheads == 0
    a \dim h = a \dim \div nheads
    k \dim h = k \dim \div nheads
    v \dim h = v \dim \div nheads
    0 = Dense(q_dim_h, gkv_dim \div nheads)
    K = Dense(k_dim_h, qkv_dim÷nheads)
    V = Dense(v_dim_h, gkv_dim÷nheads)
    D = Dense(gkv_dim,out_dim+nheads)
    MHA(Q,K,V,D,nheads)
end MHA
Flux.@functor MHA 🗸
```

```
function (mha ::MHA)(g.k.v)
    Q,K,V,D = mha.Q,mha.K,mha.V,mha.D
    qh = reshape(q, size(q, 1); mha.nheads)
    mha.nheads,size(q,2),size(q,3))
    kh = reshape(k,size(k,1)+mha.nheads,
    mha.nheads,size(k,2),size(k,3))
    vh = reshape(v,size(v,1);mha.nheads,
    mha.nheads,size(v,2),size(v,3))
    aval = 0(ah)
    kval = K(kh)
    vval = V(vh)
    @tullio att[n,m,hi,b] := gval[i,hi,n,
    b] * kval[i,hi,m,b] / sqrt(size(kval,
    1))
    att = Flux.softmax(att)
    @tullio res[i,hi,n,b] := att[n,m,hi,
    b] * vval[i,hi,m,b]
    res = reshape(res,size(res,1)*size
    (res,2),size(v)[2:end]...)
    return D(res), att
end J
```

```
x = rand(64,100,1000);
mha = MultiHeadAttention((64,64,64)
=>1024=>64,nheads = 4);
res,att= mha(x);
res 64×100×1000 Array{Float32, 3}:
att 100×100×4×1000 Array{Float32, 4}:
```

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• A lot of "usual" datasets can be directly dowload within julia and MLDatasets.



JuliaML MLDatasets.jl https://github.com/ JuliaML/MLDatasets.il JuliaPy PythonCall.jl https://github.com/ JuliaPy/PythonCall.il JuliaStats RDatasets.jl https://github.com/ JuliaStats/RDatasets.il 33/38

- A lot of "usual" datasets can be directly dowload within julia and MLDatasets.
- We always want more, and we can get more from python (PythonCall.jl) or R (Rdatasets.jl).





JuliaML MLDatasets.jl https://github.com/ JuliaML/MLDatasets_il JuliaPy PythonCall.jl https://github.com/ JuliaPy/PythonCall.jl JuliaStats RDatasets.jl https://github.com/ JuliaStats/RDatasets.il 33/38

Comparaison of including datasets

```
using MLDatasets: Iris | \/
iris = Iris(); | \/
datass = iris.features; | \/
target = iris.targets |> Array; | \/
target = reshape(target,length(target)); | \/
target = Dict("$(target[i])"=> target .== target[i] for i in
eachindex(target)) |> DataFrame | 150×3 DataFrame
```

using PythonCall // skl = PythonCall.pyimport("sklearn.datasets"); // datass, target = skl.toad_iris(return_X_y=true, as_frame=true); // using DataFrames // k = datass.koye(); // v = pyconvert(Array,datass.values); // datass = Dict([pyconvert(String,k[i-1]) => vv[:,i] for i in axes(vv,2)]...) |> DataFrame [150×4 DataFrame k= pyconvert(Array,target.teys()); // target = Dict(["\$(target[i])=> target == target[i] for i in eachindex(target)]...) |> DataFrame [150×3 DataFrame

```
using RDatasets | /

iris = RDatasets.dataset("datasets",

"iris") |150×5 DataFrame

datass = iris[:,1:4] |> Array; | /

target = iris[:,5] |> Array; | /

target = Dict("$(target[i])"=> target .

== target[i] for i in eachindex

(target) |> DataFrame |150×3 DataFrame
```

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Showcase of CNN and Transformers

Code is available on https://github.com/yolhan83.

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- Easy to make new layer, loss, optimiser, ect.
- Datasets are fully available in julia.
- Complex models can be written in a comprehensive way.
- Thank you all for your attention.